

1. -5, 1, and 2

$$(x+5)(x-1)(x-2) = 0$$

$$(x^2 + 4x - 5)(x-2) = 0$$

$$\begin{array}{r} \cancel{x^2} - \cancel{2x^2} + \cancel{4x^2} - \cancel{8x} - \cancel{5x} + 10 \\ \hline x^3 + 2x^2 - 13x + 10 \end{array}$$

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2. -3, -1, and 0

$$x(x+3)(x+1) = 0$$

$$x(x^2 + 4x + 3)$$

$$x^3 + 4x^2 + 3x$$

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3. 1, 4, and 5

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4. -2, 3, and 6

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Find the roots of the equation  $x^4 - 3x^3 + 6x^2 - 12x + 8 = 0$ .  $\pm 1, 2, 4, 8$

7. Possible roots:  $\pm 1, \pm 2, \pm 4, \pm 8$

Test:  $(x-1)$  and  $(x-2)$ .

1 and 2 are real roots.

Solve  $x^2 - 3x + 2$  to find the remaining roots.

Remaining roots:  $2i$  and  $-2i$

$$x^2 - 3x + 2 \quad \begin{array}{r} x^2 + 0x + 4 \\ \hline x^4 - 3x^3 + 6x^2 - 12x + 8 \\ \underline{x^4 - 3x^3 + 2x^2} \\ 4x^2 - 12x + 8 \end{array}$$

$$x^2 + 4 = 0$$

$$\sqrt{x^2} = \sqrt{-4}$$

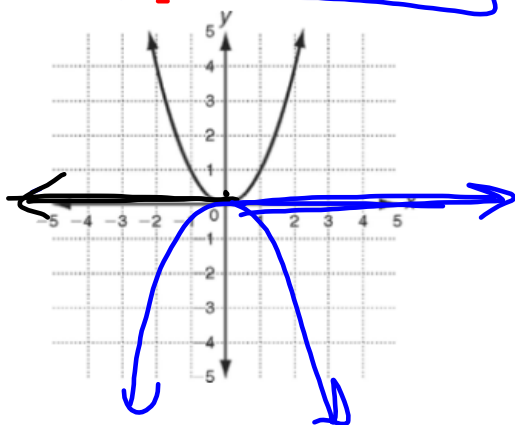
$$x = \pm 2i$$

$$\begin{array}{r} 4x^2 - 12x + 8 \\ \underline{4x^2 - 12x + 8} \\ 0 \end{array}$$

$$\begin{array}{r} 1 \quad -3 \quad 6 \quad -12 \quad 8 \\ \underline{1 \quad -2 \quad 4 \quad -8} \\ 1 \quad -2 \quad 4 \quad -8 \quad 0 \\ \underline{1 \quad -2 \quad 4 \quad -8} \\ 0 \quad 0 \quad 0 \quad 0 \quad 0 \end{array}$$

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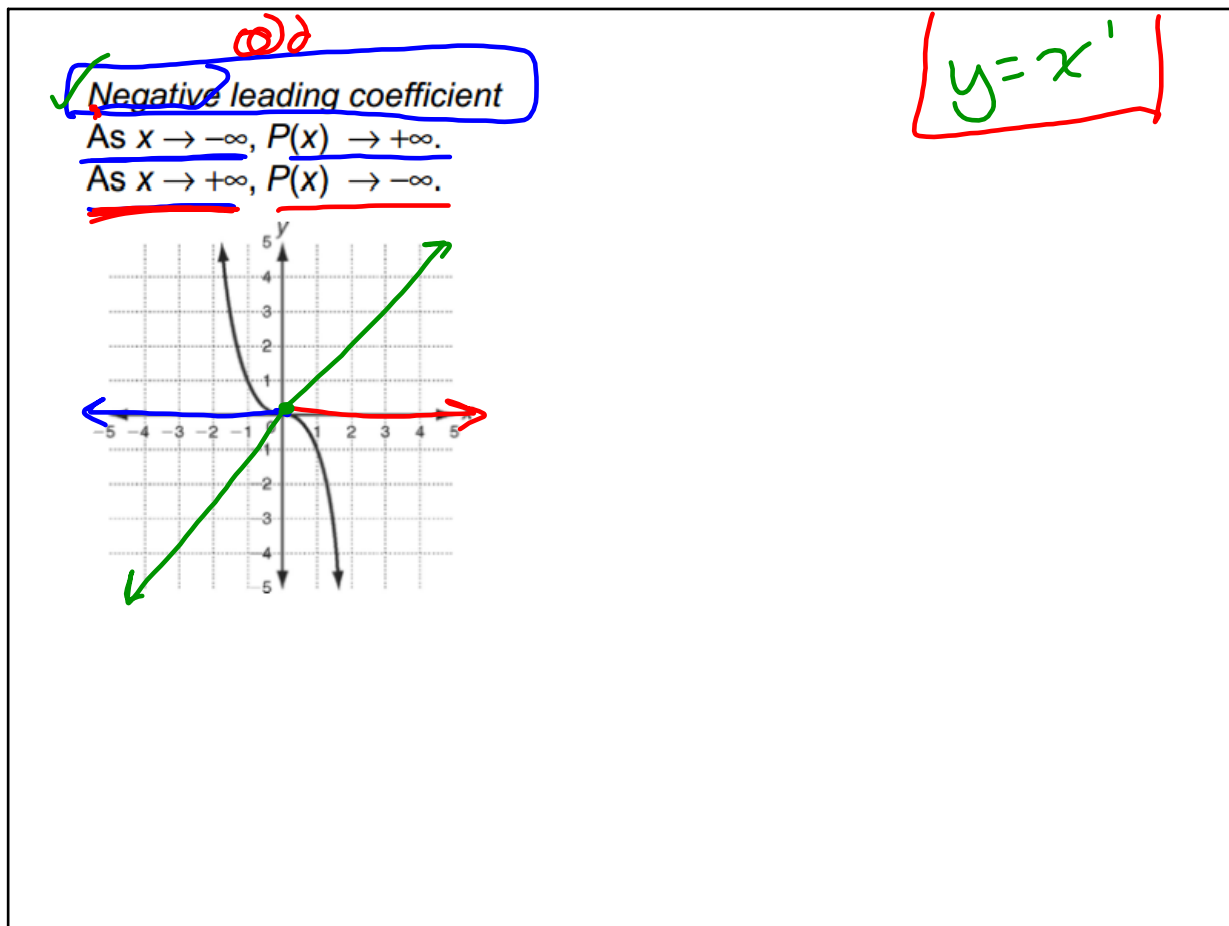
Even  
Positive leading coefficient  
As  $x \rightarrow -\infty, P(x) \rightarrow +\infty$ .  
As  $x \rightarrow +\infty, P(x) \rightarrow +\infty$ .



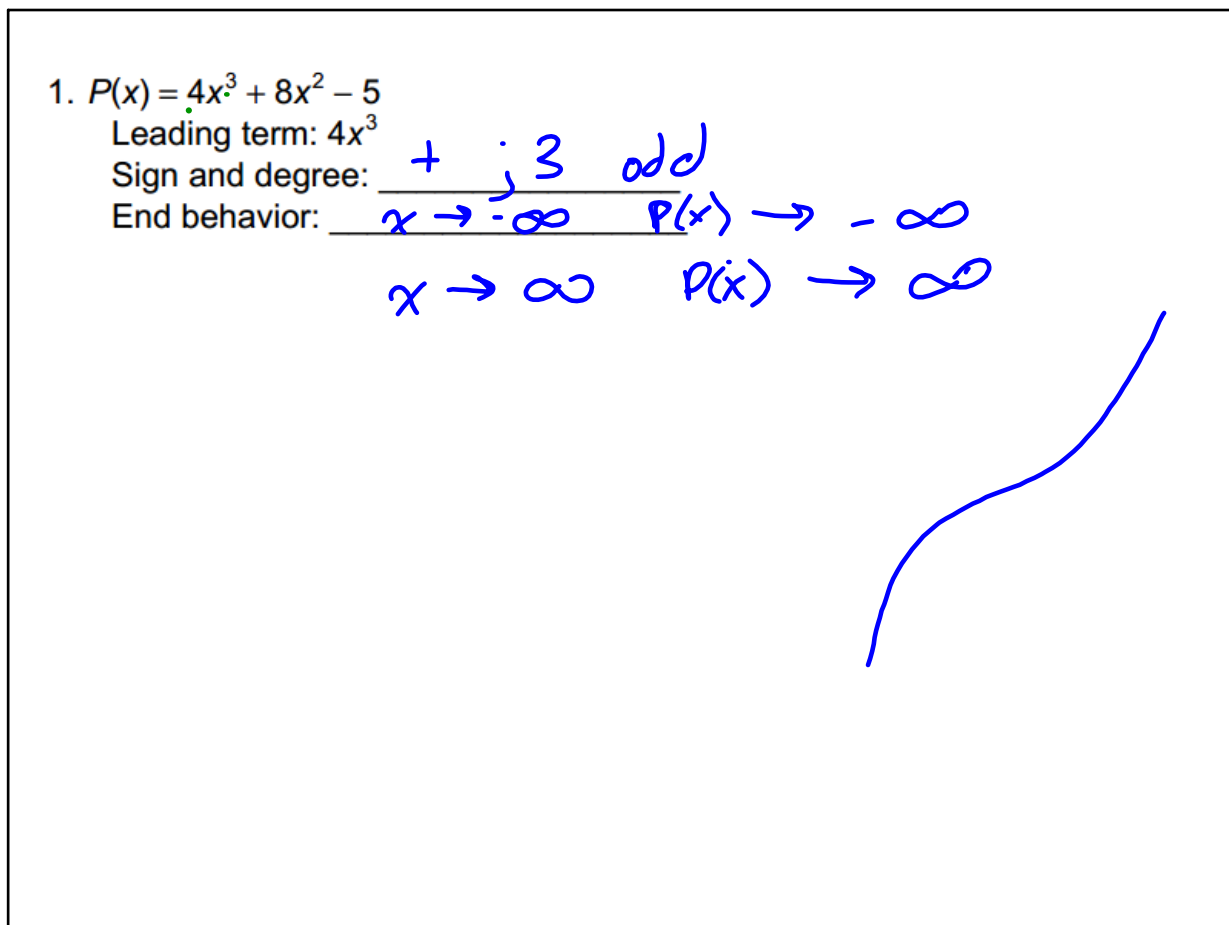
$$-2x^{24}$$

$$3x^{12}$$

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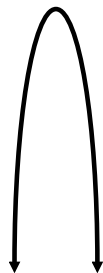
2.  $P(x) = -9x^6 + 2x^3 - x + 7$

Leading term:  $-9x^6$

Sign and degree: neg | 6 | even

End behavior:  $x \rightarrow -\infty$   $P(x) \rightarrow -\infty$

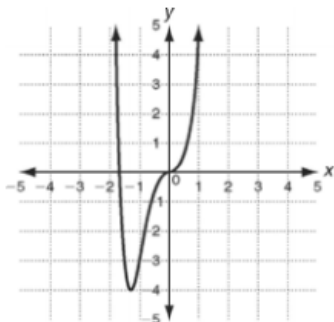
$x \rightarrow \infty$   $P(x) \rightarrow -\infty$



$\swarrow$   
 $-\infty$

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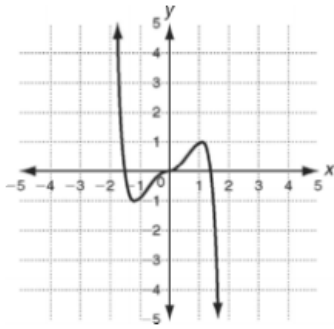
3.



even  
(+) leading coef.

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4.



$$x=0$$

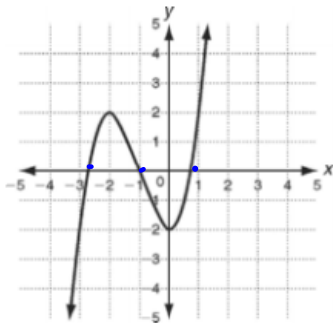
odd

(-) leading  
coeff.

$$y=x$$

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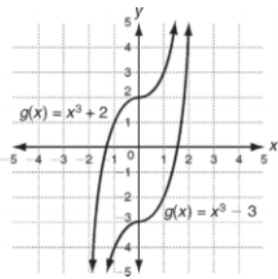
5.



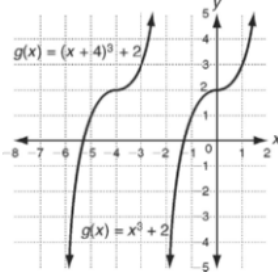
odd

(+)

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<b>Vertical Translation</b>	
<p>If <math>f(x)</math> is a polynomial function,  <math>g(x) = f(x) + k</math> is a vertical translation of <math>f(x)</math>.  <i>Example: <math>f(x) = x^3 + 2</math></i></p>	<p>Think: Add to <math>y</math>, go high.  <math>f(x)</math> shifts up for <math>k &gt; 0</math>.  <math>f(x)</math> shifts down for <math>k &lt; 0</math>.</p>
<p>Vertical translation 5 units down  <math>g(x) = f(x) - 5</math>  <math>g(x) = x^3 + 2 - 5</math>  <math>g(x) = x^3 - 3</math></p>	

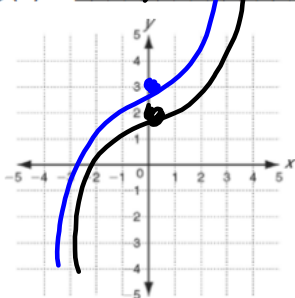
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<b><u>Horizontal Translation</u></b>	
<p>If <math>f(x)</math> is a polynomial function,  <math>g(x) = f(x - h)</math> is a horizontal translation of <math>f(x)</math>.  <i>Example: <math>f(x) = x^3 + 2</math></i></p>	<p>Think: Add to <math>x</math>, go west.  <math>f(x)</math> shifts right for <math>h &gt; 0</math>.  <math>f(x)</math> shifts left for <math>h &lt; 0</math>.</p>
<p>Horizontal translation 4 units left  <math>g(x) = f(x - (-4))</math>  <math>g(x) = (x + 4)^3 + 2</math></p>	

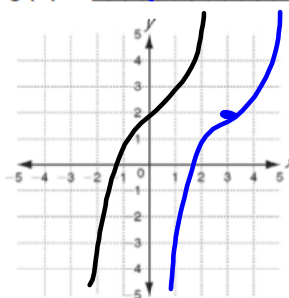
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For  $f(x) = x^3 + 2$ , write the rule for each function and sketch its graph.

1.  $g(x) = f(x) + 1$       $x^3 + 2 + 1$   
 Translate  $f(x)$  1 unit UP.  
 $g(x) = x^3 + 3$



2.  $g(x) = f(x - 3)$   
 Translate  $f(x)$  3 units Right.  
 $g(x) = (x - 3)^3 + 2$



$f(x - 3) = (x - 3)^3 + 2$

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**Vertical Stretch or Compression**

If  $f(x)$  is a polynomial function,  
 $g(x) = af(x)$  is a vertical stretch or  
 compression of  $f(x)$ .

Example:  $f(x) = 2x^4 - 6x^2 + 4$

Vertical stretch if  $a > 1$

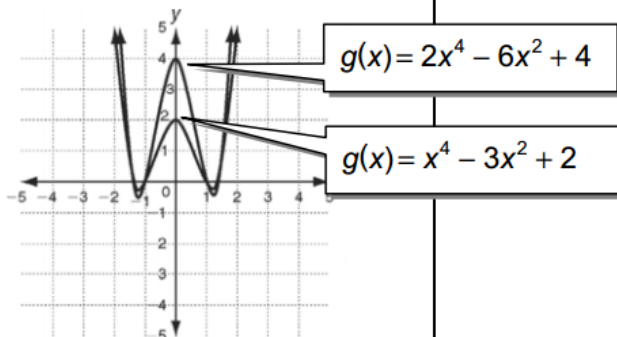
Vertical compression if  $0 < a < 1$

Vertical compression of  $f(x)$

$g(x) = \frac{1}{2}f(x)$

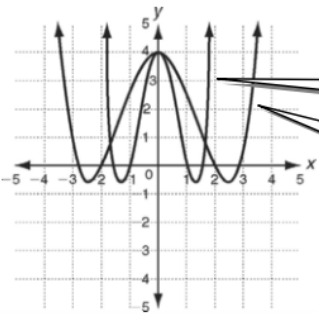
$g(x) = \frac{1}{2}(2x^4 - 6x^2 + 4)$

$g(x) = x^4 - 3x^2 + 2$



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Horizontal Stretch or Compression	
<p>If <math>f(x)</math> is a polynomial function,  <math>g(x) = f\left(\frac{1}{b}x\right)</math> is a horizontal stretch  or compression of <math>f(x)</math>.  <i>Example:</i> <math>f(x) = 2x^4 - 6x^2 + 4</math></p>	<p>Horizontal stretch if <math>b &gt; 1</math>  Horizontal compression if <math>0 &lt; b &lt; 1</math></p>
<p>Horizontal stretch of <math>f(x)</math>  <math>g(x) = f\left(\frac{1}{2}x\right)</math>  <math>g(x) = 2\left(\frac{1}{2}x\right)^4 - 6\left(\frac{1}{2}x\right)^2 + 4</math>  <math>g(x) = \frac{1}{8}x^4 - \frac{3}{2}x^2 + 4</math></p>	 <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 5px;"> <math>g(x) = 2x^4 - 6x^2 + 4</math> </div> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 5px;"> <math>g(x) = \frac{1}{8}x^4 - \frac{3}{2}x^2 + 4</math> </div>

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Let  $f(x) = 2x^4 - 6x^2 + 4$ . Describe  $g(x)$  as a transformation of  $f(x)$  and write the rule for  $g(x)$ .

3.  $g(x) = 2f(x)$

4.  $g(x) = f(2x)$

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Use finite differences to determine the degree of the polynomial that best describes the data.

1.

$x$	-2	-1	0	1	2
$y$	-5	2	3	4	11
First Differences		+7	+1	+1	+7
Second Differences		-6	+0	+6	
Third Differences		+6	+6		

2. Identify the degree of the polynomial.

cubic

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Write a polynomial function for the data.

3.

$x$	2	4	6	8	10	12
$y$	-12	-15	38	190	446	773
First Differences		-3	+53	+152	+256	+327
Second Differences		+56	+99	+104	+71	
Third Differences		43	+5	-33		
Fourth Differences			-38	-38		

4. Write a polynomial function that best describes the data set.

Quartic

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